

# UNCLASSIFIED

AD NUMBER
ADB012953
NEW LIMITATION CHANGE
TO Approved for public release, distribution unlimited
FROM Distribution authorized to U.S. Gov't. agencies only; Test and Evaluation; AUG 1976. Other requests shall be referred to Ballistic Research Labs., Aberdeen Proving Ground, MD.
AUTHORITY
BRL ltr, 13 Nov 1986

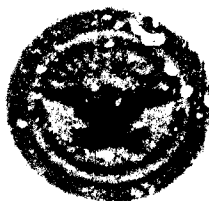
THIS PAGE IS UNCLASSIFIED

AD Bo 12953

AUTHORITY:

BCL etc.

13 NOV 64



THIS REPORT HAS BEEN DELIMITED  
AND CLEARED FOR PUBLIC RELEASE  
UNDER DOD DIRECTIVE 5200.20 AND  
NO RESTRICTIONS ARE IMPOSED UPON  
ITS USE AND DISCLOSURE.

DISTRIBUTION STATEMENT A

APPROVED FOR PUBLIC RELEASE;  
DISTRIBUTION UNLIMITED.

✓  
BRL MR 2649

② 11  
BRL

AD

MEMORANDUM REPORT NO. 2649

ELASTIC CONSTANTS OF ALUMINUM ALLOYS,  
2024-T3510, 5083-H131 AND 7039-T64 AS  
MEASURED BY A SONIC TECHNIQUE

Ralph F. Benck  
Gordon L. Filbey, Jr.

DDC  
RECEIVED  
AUG 20 1976  
NEGATIVE

JS

A

August 1976

Distribution limited to US Government agencies only; Test and  
Evaluation; Aug 76. Other requests for this document must be  
referred to Director, USA Ballistic Research Laboratories,  
ATTN: DXBR-TS, Aberdeen Proving Ground, Maryland 21005.

AD NO. \_\_\_\_\_  
DDC FILE COPY

USA BALLISTIC RESEARCH LABORATORIES  
ABERDEEN PROVING GROUND, MARYLAND

12  
Destroy this report when it is no longer needed.  
Do not return it to the originator.

Secondary distribution of this report by originating  
or sponsoring activity is prohibited.

Additional copies of this report may be obtained  
from the Defense Documentation Center, Cameron  
Station, Alexandria, Virginia 22314.

The findings in this report are not to be construed as  
an official Department of the Army position, unless  
so designated by other authorized documents.

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS MAY BE COMPLETING FORM
1. REPORT NUMBER BRL Memorandum Report No. 2649	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) Elastic Constants of Aluminum Alloys, 2024-T3510, 5083-H131 and 7039-T64 as Measured by a Sonic Technique.	5. TYPE OF REPORT & PERIOD COVERED Final rept.	
7. AUTHOR(s) Ralph P. Benck Gordon L. Filbey, Jr	6. PERFORMING ORG. REPORT NUMBER	
8. PERFORMING ORGANIZATION NAME AND ADDRESS US Army Ballistic Research Laboratories Aberdeen Proving Ground, MD 21005	9. CONTRACT OR GRANT NUMBER(s)	
11. CONTROLLING OFFICE NAME AND ADDRESS US Army Materiel Development & Readiness Command 5001 Eisenhower Avenue Alexandria, VA 22333	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS RDT&E Proj. No. 1T161102A33H	
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) 1222p.	12. REPORT DATE AUG 1976	
	13. SECURITY CLASS. (of this report) Unclassified	
	15. DECLASSIFICATION/DOWNGRADING SCHEDULE	
16. DISTRIBUTION STATEMENT (of this Report) Distribution limited to US Government agencies only; Test and Evaluation; August 1976. Other requests for this document must be referred to Director, USA Ballistic Research Laboratories, ATTN: DRXBR-TS, Aberdeen Proving Ground, MD 21005.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report) BRL-MR-2649		
18. SUPPLEMENTARY NOTES RDT/E-1-T-161102-A-33-H		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) armor                      sonic testing Poisson's ratio          aluminum alloys Young's modulus        shear modulus		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number)    bet This report presents the results of sonic tests performed on aluminum alloys, 2024-T3510, 5083-H131 and 7039-T64. Young's modulus, the shear modulus, Poisson's ratio and the velocity of sound are reported for the temperature range of 22° to 550°C.		

# TABLE OF CONTENTS

	<u>Page</u>
TABLE OF CONTENTS . . . . .	3
I. INTRODUCTION. . . . .	5
II. EXPERIMENTS . . . . .	5
A. Apparatus . . . . .	5
B. Specimens . . . . .	6
C. Procedure . . . . .	6
D. Calculations. . . . .	7
III. RESULTS AND DISCUSSION. . . . .	9
IV. CONCLUSIONS . . . . .	11
REFERENCES. . . . .	22
DISTRIBUTION LIST . . . . .	23

ACCESSION for	
NTIS	Whole Section <input type="checkbox"/>
DOC	Entire Section <input checked="" type="checkbox"/>
UNCLASSIFIED	<input type="checkbox"/>
DISSEMINATION	

B

## I. INTRODUCTION

The sonic tests reported herein were conducted in connection with the Core Materials Program of the Solid Mechanics Branch of the Terminal Ballistics Laboratory.

The purpose of the Core Materials Program is to characterize the mechanical behavior of armor and armor penetrator materials. This characterization should prove useful to the designers of armored vehicles and projectiles and will provide valuable input data for computer codes that model penetration processes.

The present report concerns itself with dynamic sonic testing of three aluminum alloys, used as either structural or armor material. The results reported herein consist of Young's modulus (E), the shear modulus (G), and Poisson's ratio ( $\nu$ ) as a function of temperature.

## II. EXPERIMENTS

The measurement method is the resonance type i.e., when made to vibrate by a suitable transducer, the test specimen will resonate at a preferred vibrational frequency. This frequency is dependent upon the physical dimensions, density and modulus of elasticity of the sample. If the driving force is provided at a frequency which corresponds to the resonant frequency of the sample, then the amplitude of oscillation will be relatively high and "resonance" occurs. When this is achieved the sound waves introduced and reflected from the end of the sample retrace their original path and set up reinforcement with following waves. Quick and accurate determination of the frequency of these waves is relatively easy.

### A. APPARATUS

The device used to measure the natural resonant frequencies of the test specimen is a precision, electronic, sonic test instrument: a Magnaflux Model SR-200 Elastomat, made by the Magnaflux Corporation of Chicago, Illinois. The frequency range of the oscillator is 500 Hz to 50 kHz with frequency stability reported to be within 0.01 percent.<sup>1\*</sup> Piezoelectric transducers are used with frequency counting times of 10 sec. ( $\pm 1$  count). For measurements made at elevated temperatures, a Magnaflux high temperature furnace (Model 204528) and furnace control console (Model 98176) are used. The maximum furnace temperature is 1000°C with a chamber temperature uniformity reported<sup>1</sup> to be  $\pm 1.1^\circ\text{C}$  for a six-inch center zone.

\*References are listed on page 22.



## B. SPECIMENS

Test specimens were machined into the form of nominally 6-inch long, 3/8-inch diameter rods. The physical dimensions of the specimens tested are listed in Table I. All the test specimens originated from heats of metal that previously had been the source of compression samples for quasi-static stress-strain curves.<sup>2,3,4</sup> The chemical analyses of the alloys are included in References 2, 3, and 4.

TABLE I

### PHYSICAL PROPERTIES OF 3/8-INCH DIAMETER SPECIMENS

Alloy	Sample Number	Length cm	Weight g	Apparent* Density g cm <sup>-3</sup>
2024-T3510	1-1	15.22	30.2486	2.789
"	1-2	15.24	30.2423	2.785
"	1-3	15.24	30.2889	2.789
"	1-4	15.24	30.2855	2.789
5083-H131	2-1	15.24	28.9655	2.667
"	2-2	15.24	28.9706	2.668
"	2-3	15.24	28.9506	2.666
"	2-4	15.24	28.9240	2.664
7039-164	3-1	15.12	29.4506	2.734
"	3-2	15.37	30.0490	2.744
"	3-3	15.24	29.8535	2.749

\*Ratio of weight to specimen volume.

## C. PROCEDURE

The specimen is suspended on a support cradle with a piezoelectric driver transducer attached to one end and a receiver transducer attached to the other. For measurements at elevated temperatures, the support cradle was placed in a uniformly hot zone of a furnace. Initially, the thin wire ends of the transducers were put in prick marks on the ends of the specimens and kept in place by flexure of the wire. At elevated temperatures the wires tended to sag and slip off the specimen. To prevent this, the transducer wires were spot welded to the ends of the specimens. This arrangement worked satisfactorily, except that the spot-weld generally broke at temperatures greater than 550°C.

The procedure used to measure the frequencies as a function of temperature is as follows: (1) Determine resonant frequencies at room temperature, (2) increase furnace temperature by either 25 or 50°C, (3) wait 25 minutes, (4) determine resonant frequencies at new temperature

and (5) repeat steps 2 through 4 until 550 or 575°C is reached. The material properties were never remeasured on a sample that had been heated and cooled because these alloys were initially in a heat-treated condition. Additional tests were made on samples 1-4 and 3-1, which had previously been heated to 575°C. These determinations were of the relative effect of duration of heating at 400°C on the modulus and not of the absolute value of the modulus itself.

#### D. CALCULATIONS

The transducer excites the sample in three modes of vibration; transverse, torsional and longitudinal.

The frequency of the longitudinal mode of vibration,  $F^L$ , is.

$$F^L = \frac{V_L}{2} \cdot \frac{1}{L} \quad (1)$$

where L = Length of test sample

$V_L$  = Velocity of sound =  $\sqrt{E/D}$

E = Modulus of Elasticity

D = Mass Density

Substituting for E in Equation (1) and using the weight, P (in grams) for a circular rod, we have

$$E = 50.9122 \cdot 10^{-8} P \frac{L}{d^2} (F^L)^2, \quad (2)$$

where E is in megapascals and L and d (the diameter of the rod) are in centimeters.

Expression (2) neglects lateral inertia. This effect has been evaluated by Rayleigh<sup>5</sup> who takes into account the effects of shape, size and Poisson's ratio. This contribution, in the form of a correction factor,  $K_1^L$ , is:

$$K_1^L = 1 + \frac{d^2}{L^2} \frac{v^2}{8} = 1 + \frac{d}{L^2} 1.2337 v^2 \quad (3)$$

v = Poisson's ratio

For circular cross-section specimens the transverse resonant frequency ( $F^T$ ) is given by:

$$F^T = \frac{V_L d}{8\pi L^2} \quad (4)$$

Solving equation (4) for E, we have

$$E = 16.0623 \cdot 10^{-8} \left( \frac{P}{L} \right) \left( \frac{L}{d} \right)^4 (F^T)^2, \quad (5)$$

A second correction factor,  $K_1^T$ , which takes into account the rotary inertia of the specimens<sup>1</sup>, is:

$$K_1^T = 1 + \frac{d^2}{L^2} (3.092 + 0.854 \frac{E}{G}) - \frac{d^4}{L^4} 2.172 \frac{E}{G} \quad (6)$$

The torsional resonant frequency ( $F^{Tor}$ ) of a circular rod is:

$$F^{Tor} = \frac{V_{Tor}}{2} \cdot \frac{1}{L} \quad (7)$$

where  $V_{Tor} = \sqrt{G/D}$

G = Shear modulus

Solving Equation (7) for G, we have:

$$G = 50.9122 \cdot 10^{-8} P \frac{L}{d^2} (F^{Tor})^2 \text{ (megapascals)} \quad (8)$$

The effect of thermal expansion of the test rod at elevated temperatures must be considered.<sup>1</sup> This is accomplished by multiplying Equations (2), (5), and (8) by the factor

$$F(t) = \frac{1}{1 + \alpha t} \quad (9)$$

where  $\alpha$  = coefficient of thermal expansion and

t = temperature.

Poisson's ratio,  $\nu$ , can be calculated if E and G are known.

$$\nu = \frac{E}{2G} - 1 \quad (10)$$

Substituting Equations (2) and (8) in Eq. (10) one obtains a value for  $\nu$  based on the longitudinal and torsional frequencies so that this equation may be written as equation (11).

$$\nu = \frac{1}{2} \left( \frac{F^L}{F^{Tor}} \right)^2 - 1 \quad (11)$$

Similarly, if Equations (5) and (8) are substituted in Equation (10) one obtains a value for  $\nu$  based on the translational and torsional frequencies and is written as Equation (12).

$$\nu = 0.1577 \left( \frac{L^2}{d} \right) \left( \frac{F^T}{F_{ToL}} \right)^2 - 1 \quad (12)$$

The velocity of sound ( $\text{cm sec}^{-1}$ ) can be computed from either the transverse or the longitudinal resonant frequency by the following relationships:

$$V_L = 2LF^L \quad (13)$$

$$V_T = 1.0812 \frac{L^2}{d} F^T \quad (14)$$

### III. RESULTS AND DISCUSSION

Young's modulus (modulus of elasticity),  $E$ , the shear modulus,  $G$ , and Poisson's ratio,  $\nu$ , for the three alloys, measured at room temperature ( $22^\circ\text{C}$ ) by the dynamic sonic method, are listed in Table II. The values presented are averages of measurements made on the specimens listed in Table I. Young's modulus and Poisson's ratio can be computed by using either the longitudinal or torsional resonant frequencies and values computed from both frequencies are presented. In computing  $E(T)$ ,  $E(L)$ ,  $\nu(T)$  and  $\nu(L)$  the corrections for inertia (expressions (3) and (6)) were applied.

TABLE II  
MECHANICAL PROPERTIES OF 2024-T3510, 5083-H131  
AND 7039-T64 ALUMINUM ALLOYS AT  $22^\circ\text{C}$

Alloy	Sonic Tests					Quasi-Static Compression Tests <sup>2,3,4</sup>	
	$E(T)$ GPa	$E(L)$ GPa	$G$ GPa	$\nu(L)$	$\nu(T)$	$E$ GPa	$\nu$
2024-T3510	75.44	74.93	28.3	0.321	0.304	76.1	0.321
5083-H131	71.76	71.73	27.1	0.318	0.300	71.5	0.320
7039-T64	70.43	69.63	26.1	0.320	0.300	71.8	0.326

Table II also includes corresponding data from quasi-static compression tests of specimens from the same heats of material as used in the sonic tests

In order to determine the time necessary for temperature equilibrium to be established in a heated specimen, the following experiment was performed. A sample was placed in the furnace and the resonant transverse frequency measured at room temperature. The furnace was then turned on and the transverse frequency monitored as the sample was heated and then held at a furnace temperature of 400°C. Results of two experiments of this type are shown in Figure 1 for one specimen each of 5083-H131 and 7039-T64.

Figure 1 shows that initially there is a rapid decrease in transverse frequency as the samples are heated from room temperature (20°C) to 400°C. The frequency levels off after approximately 20 minutes in the oven, and remains fairly constant for another 60 minutes at which time it starts to slowly increase. For the elevated temperature experiments reported herein, we waited 25 minutes between temperature increase and frequency measurement. Based on the results of Figure 1 and the fact that the maximum temperature increase was 50°C and not 380°C as shown in Figure 1, the 25 minute waiting period should have been adequate for the frequencies to have reached the level portion of their response curve.

Young's modulus, the shear modulus, Poisson's ratio and the velocity of sound for the alloys tested are presented as a function of temperature in Figures 2 through 10. All these quantities were corrected for thermal expansion and inertial effects by applying expressions 9, 3 and 6, respectively. Separate curves are presented for  $E(T)$ ,  $E(L)$ ,  $\nu(T)$  and  $\nu(L)$ . The corrections reduced the differences between  $V(T)$  and  $V(L)$  to an insignificant amount and therefore the average velocities of sound are shown in Figures 4, 7 and 10.

As the temperature is increased the wave amplitudes at the resonant frequencies tend to decrease thereby making it difficult to locate those that were initially weak. This is especially true for the torsional frequencies and may explain the somewhat erratic behavior observed in Poisson's ratio at temperatures greater than 500°C.

There is not much information available in the literature concerning the temperature dependence of the elastic constants reported herein. The elastic constants of single crystal aluminum appear to vary smoothly with temperature up to near the melting point<sup>6,7</sup>. Garofalo<sup>8</sup> states that  $E$  and  $G$  for metals should vary linearly with temperature up to near the melting point, however in polycrystalline metals various types of discontinuities or deviations from linearity are found beyond certain critical temperatures. The experimental results for the aluminum alloys shown in Figures 2, 5 and 8 generally agree with the concept of linear dependence between  $E$ ,  $G$  and temperature. One study of  $E$  versus temperature (up to 370°C) for 2024-T4 and 2024-T36 sheets<sup>9</sup> presents data similar to that shown in Figure 2.

Poisson's ratio for steels<sup>8,10</sup> is reported to remain constant or to increase slightly as the temperature is raised. Data on Poisson's ratio as a function of temperature for aluminum alloys are sparse but one study<sup>11</sup> on aluminum alloy, 6061-T6, shows a linear decrease in  $\nu$  as the temperature is increased from 25°C to 200°C.

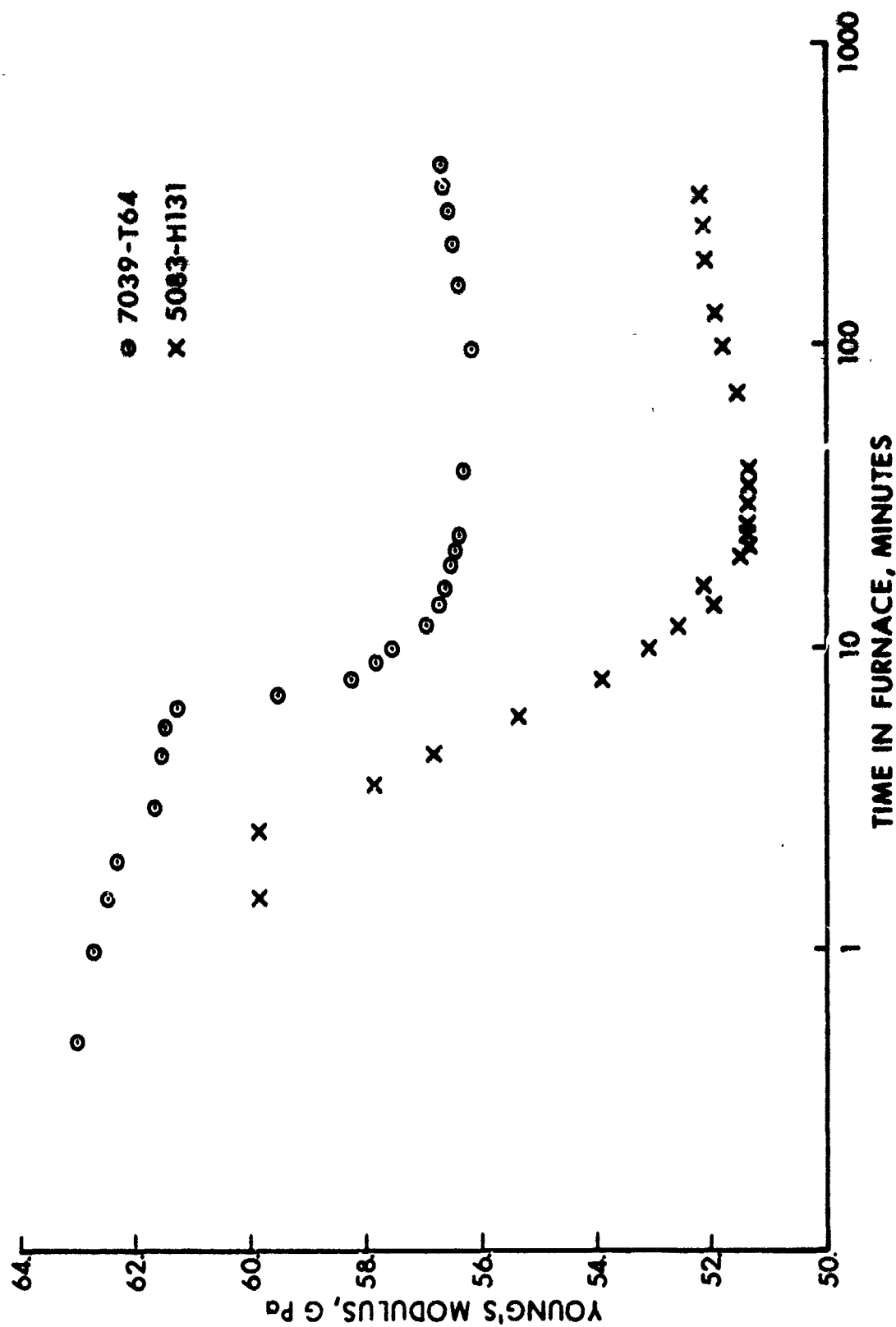


Figure 1- Young's Modulus as a Function of Time at 400°C for Alloys 7039-T64 (Sample 3-1) and 5083-H131 (Sample 1-4)

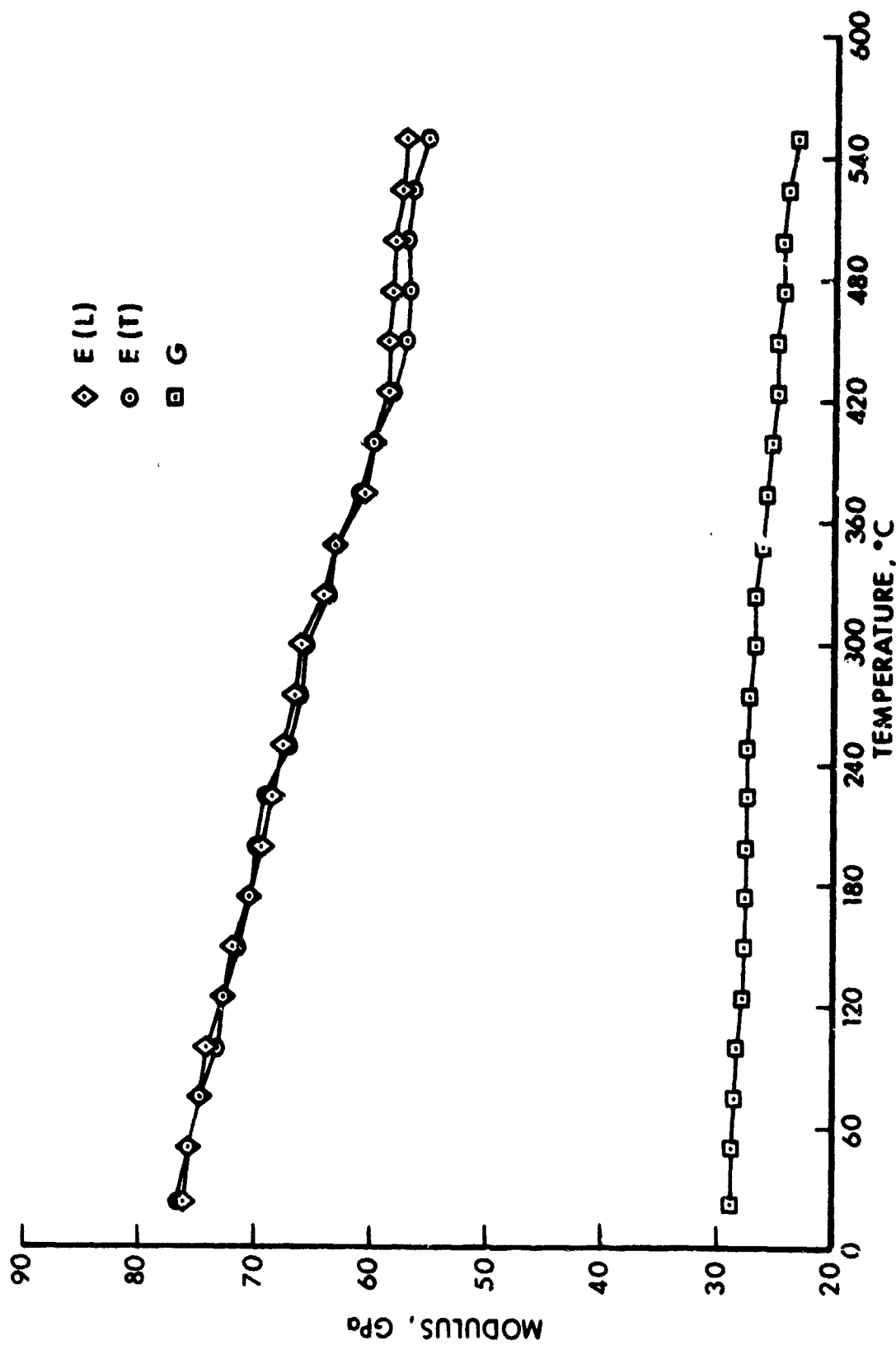


Figure 2. Young's Modulus and the Shear Modulus as a Function of Temperature for 2024-T3510 Aluminum Alloy

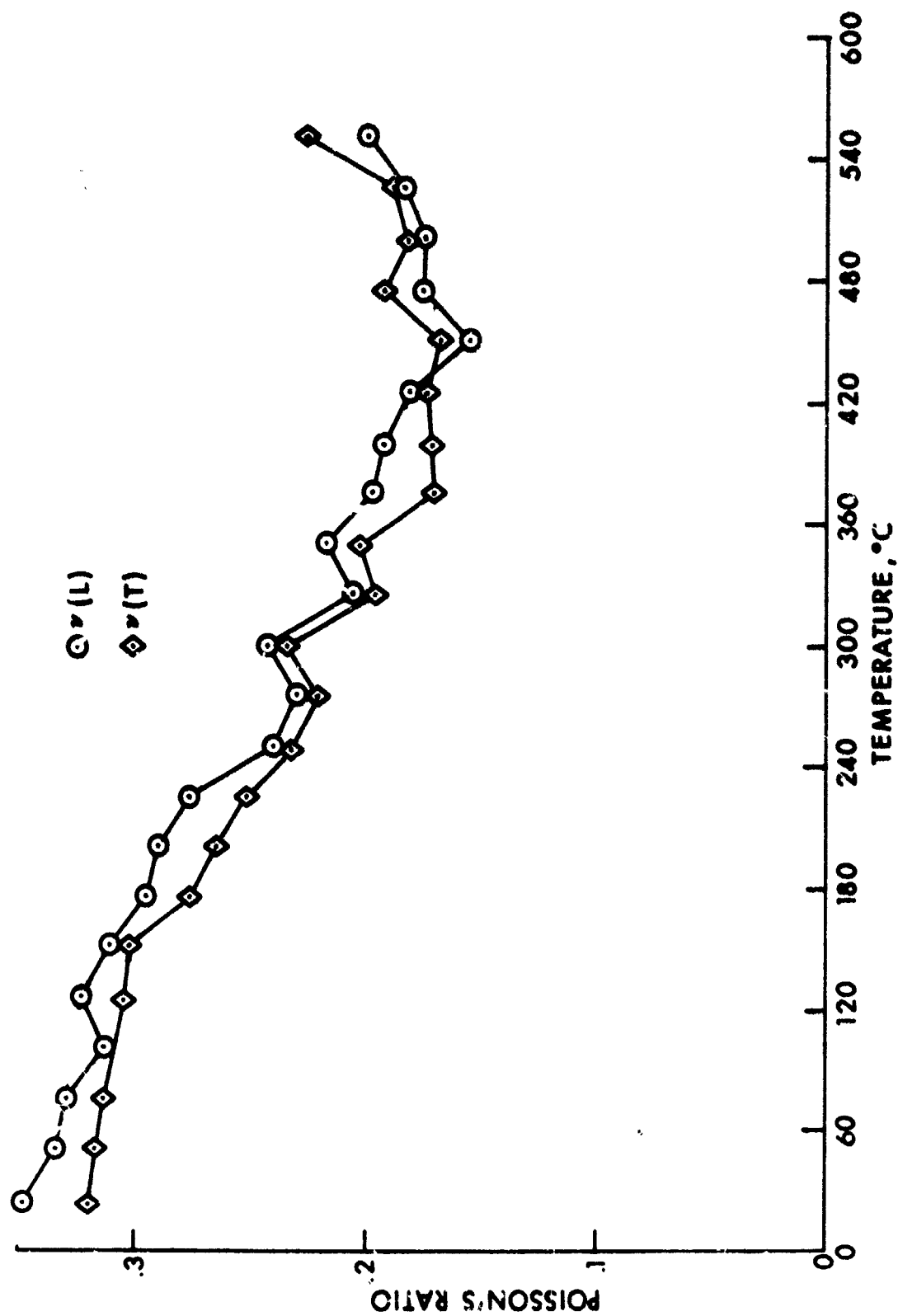
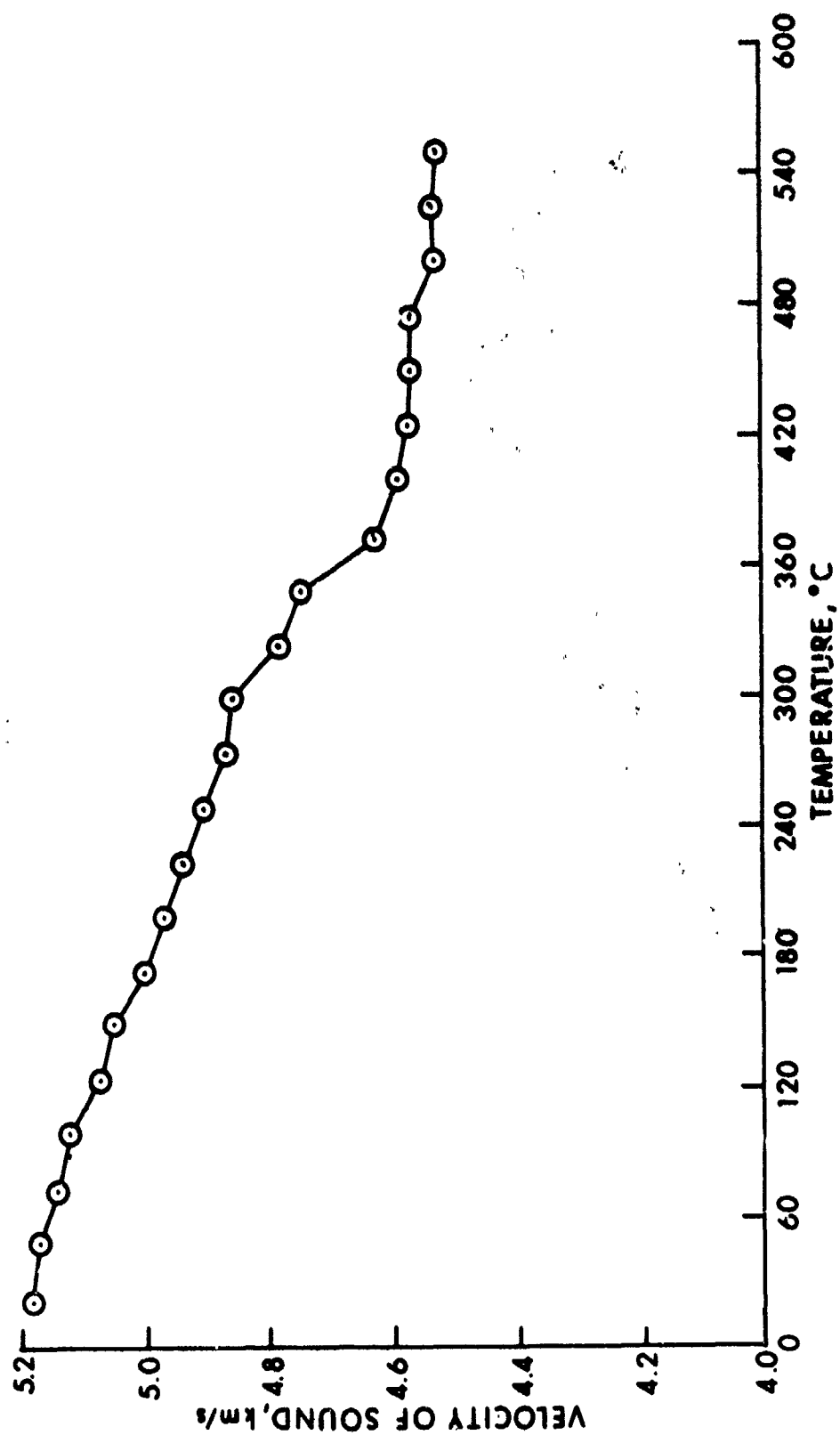


Figure 3 - Poisson's Ratio as a Function of Temperature for 2024-T3510 Aluminum Alloy.





**Figure 4 - Velocity of Sound as a Function of Temperature for 2024-T3510 Aluminum Alloy.**

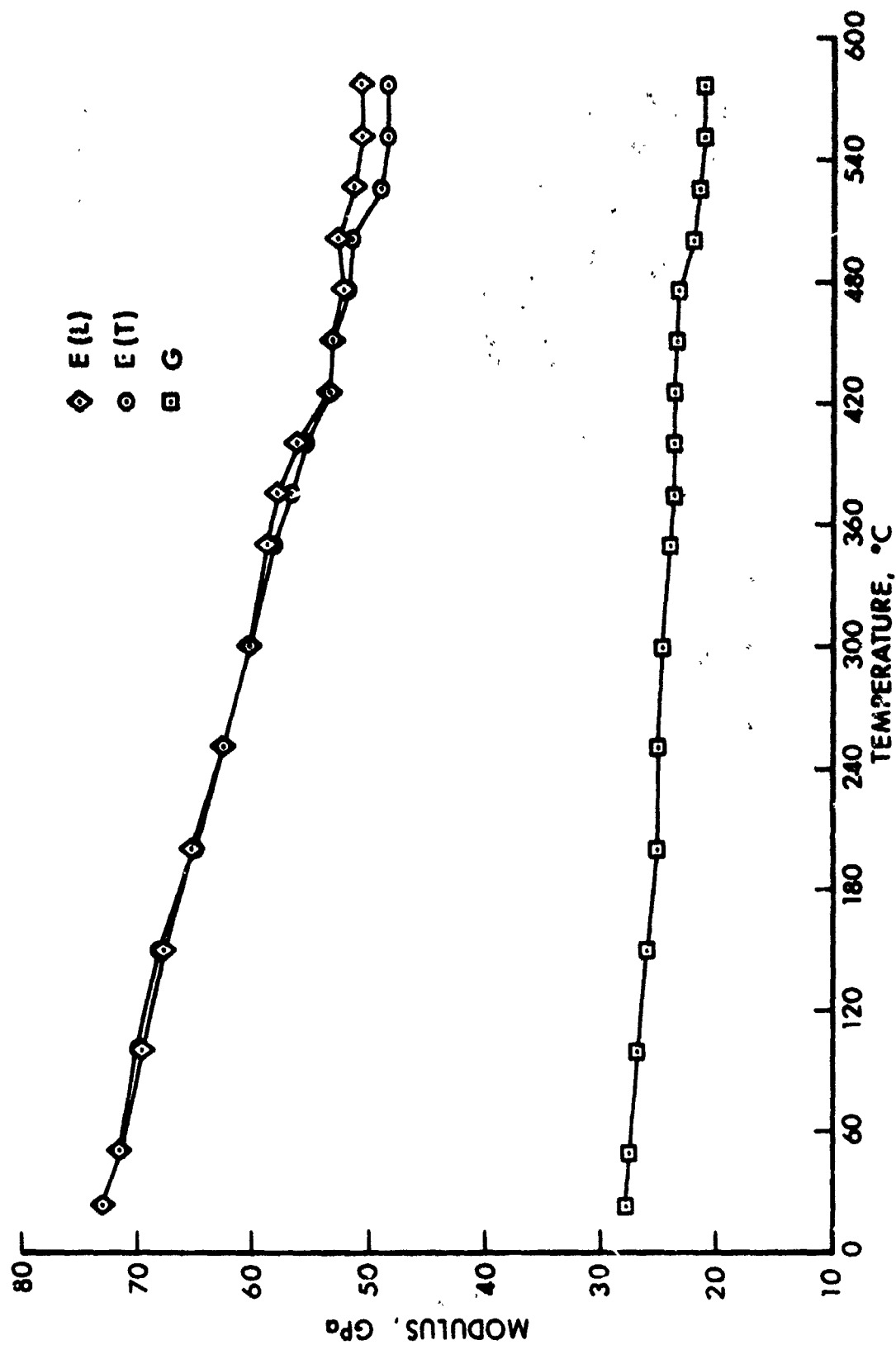


Figure 5. Young's Modulus and the Shear Modulus as a Function of Temperature for 5083-H131 Aluminum Alloy

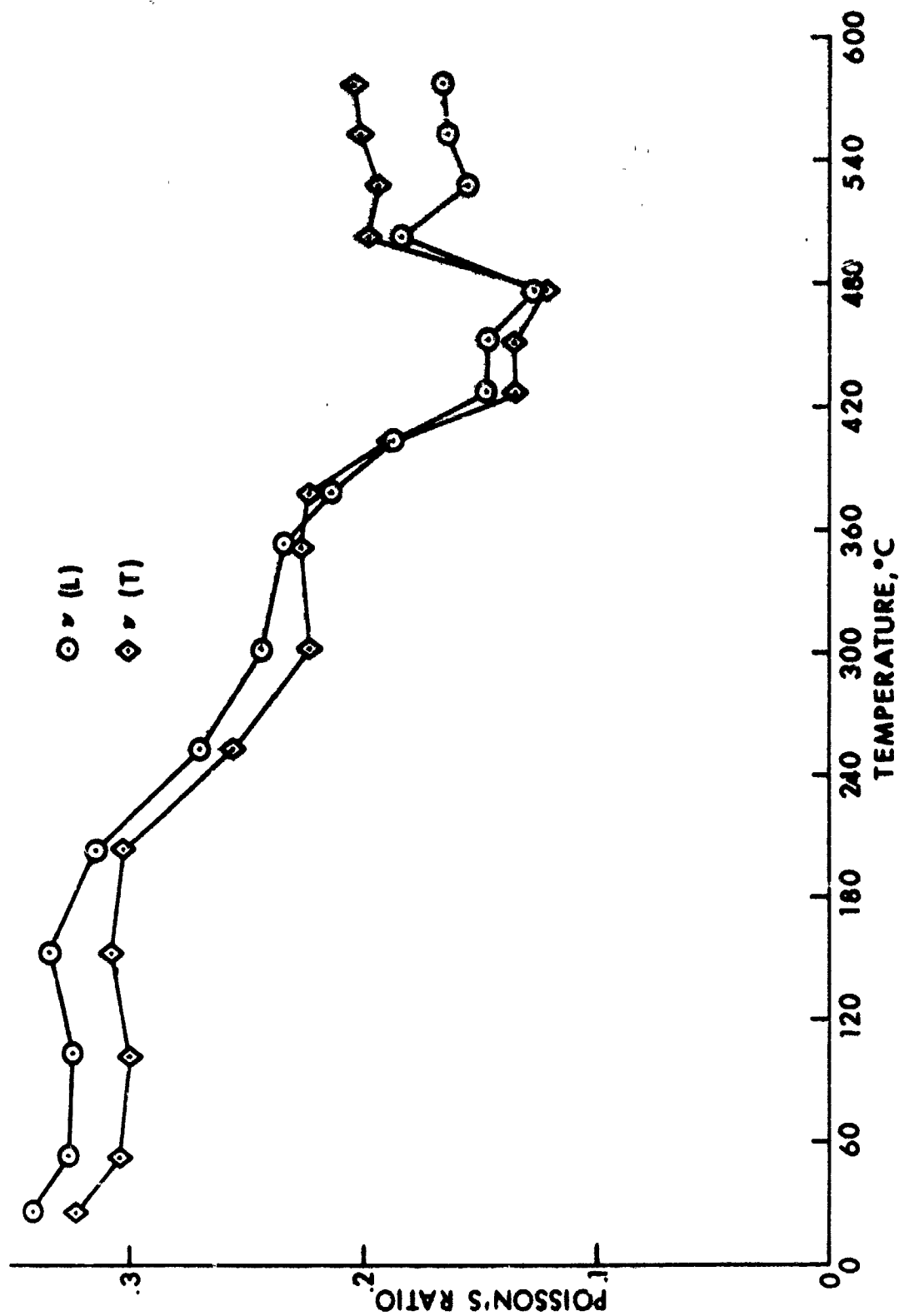
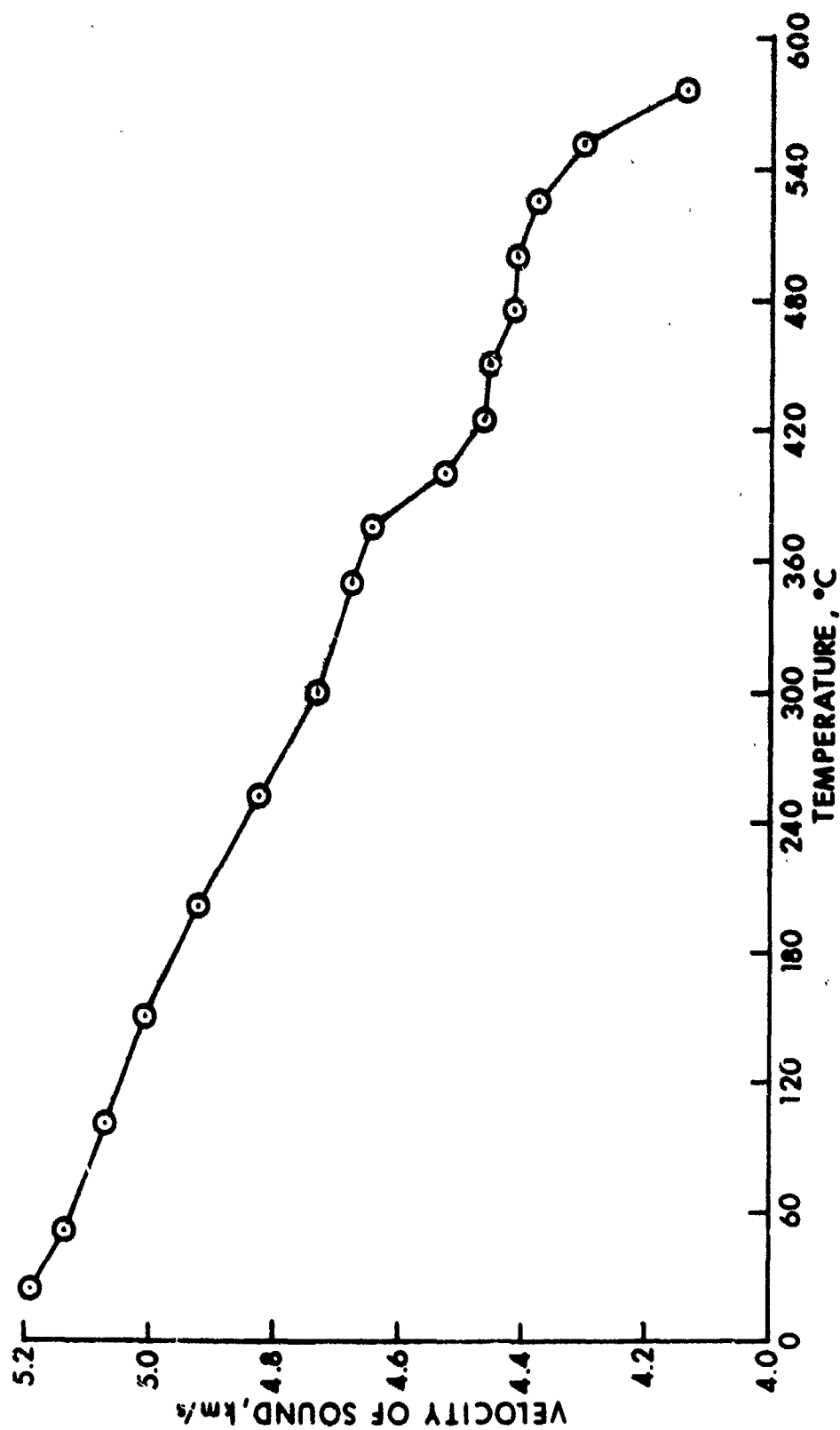


Figure 6 - Poisson's Ratio as a Function of Temperature for 5083-H131 Aluminum Alloy.



**Figure 7- Velocity of Sound as a Function of Temperature for 5083-H131 Aluminum Alloy.**

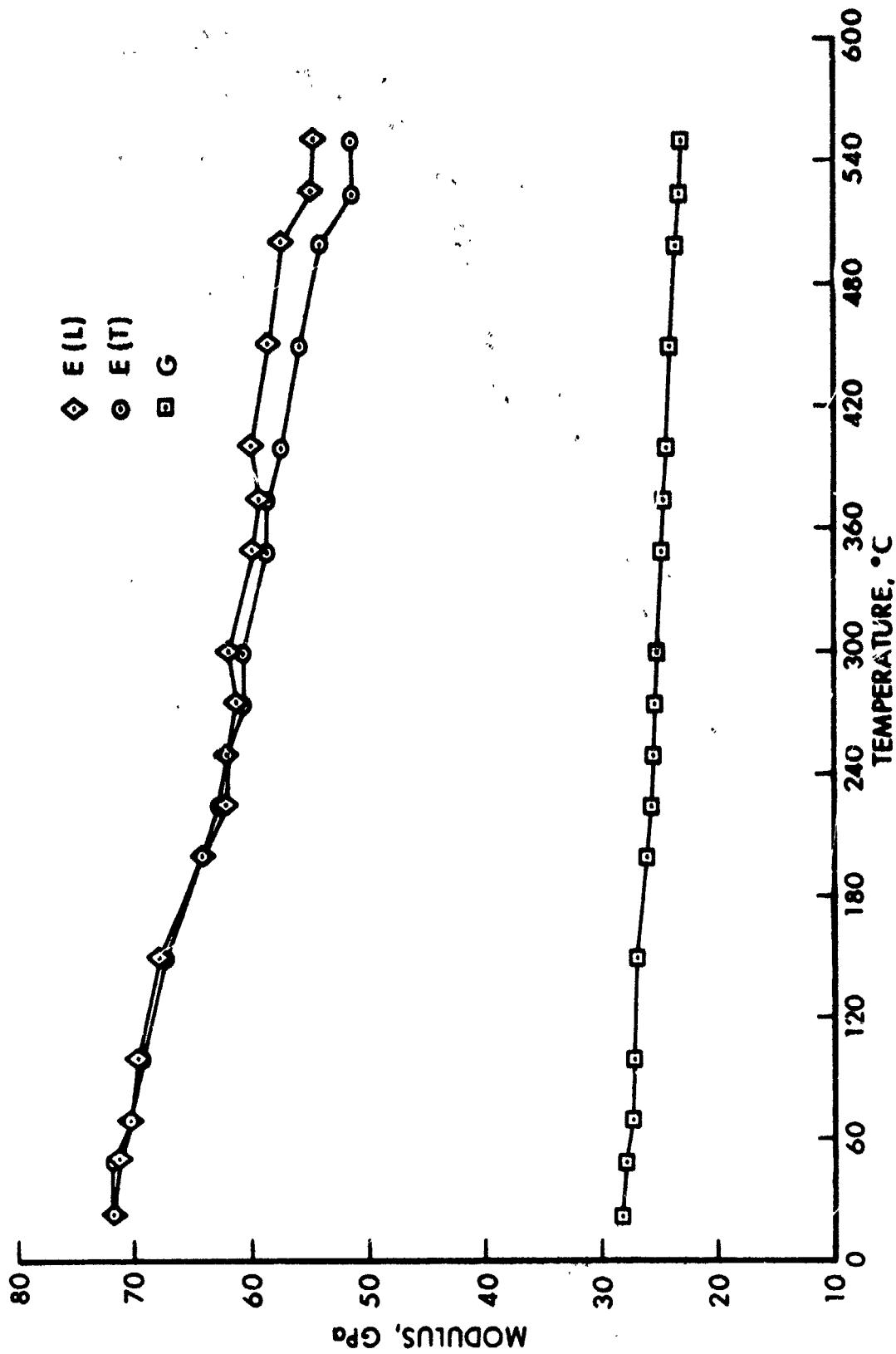


Figure 8. Young's Modulus and the Shear Modulus as a Function of Temperature for 7039-T64 Aluminum Alloy

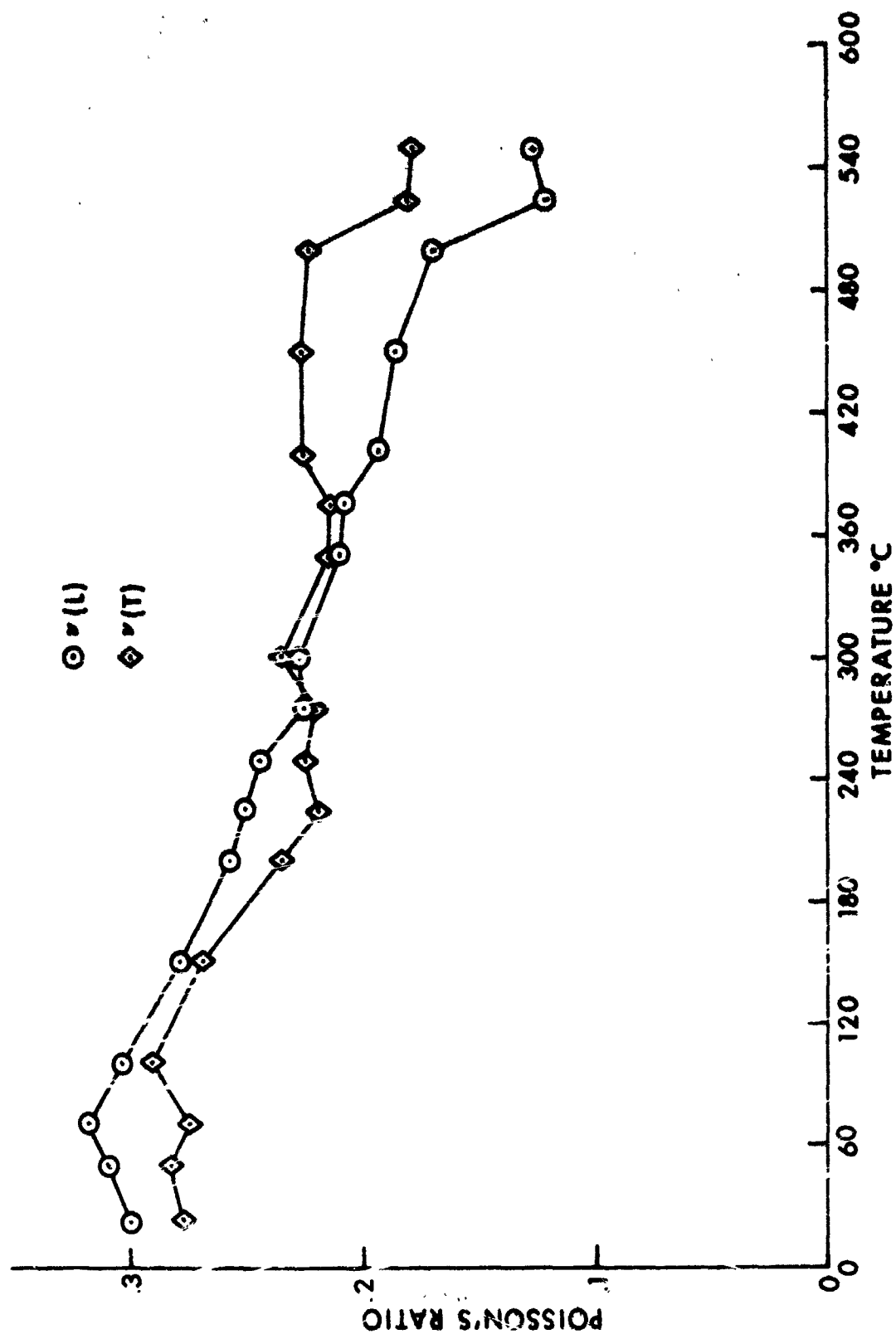


Figure 9-Poisson's Ratio as a Function of Temperature for 7039-T64 Aluminum Alloy.

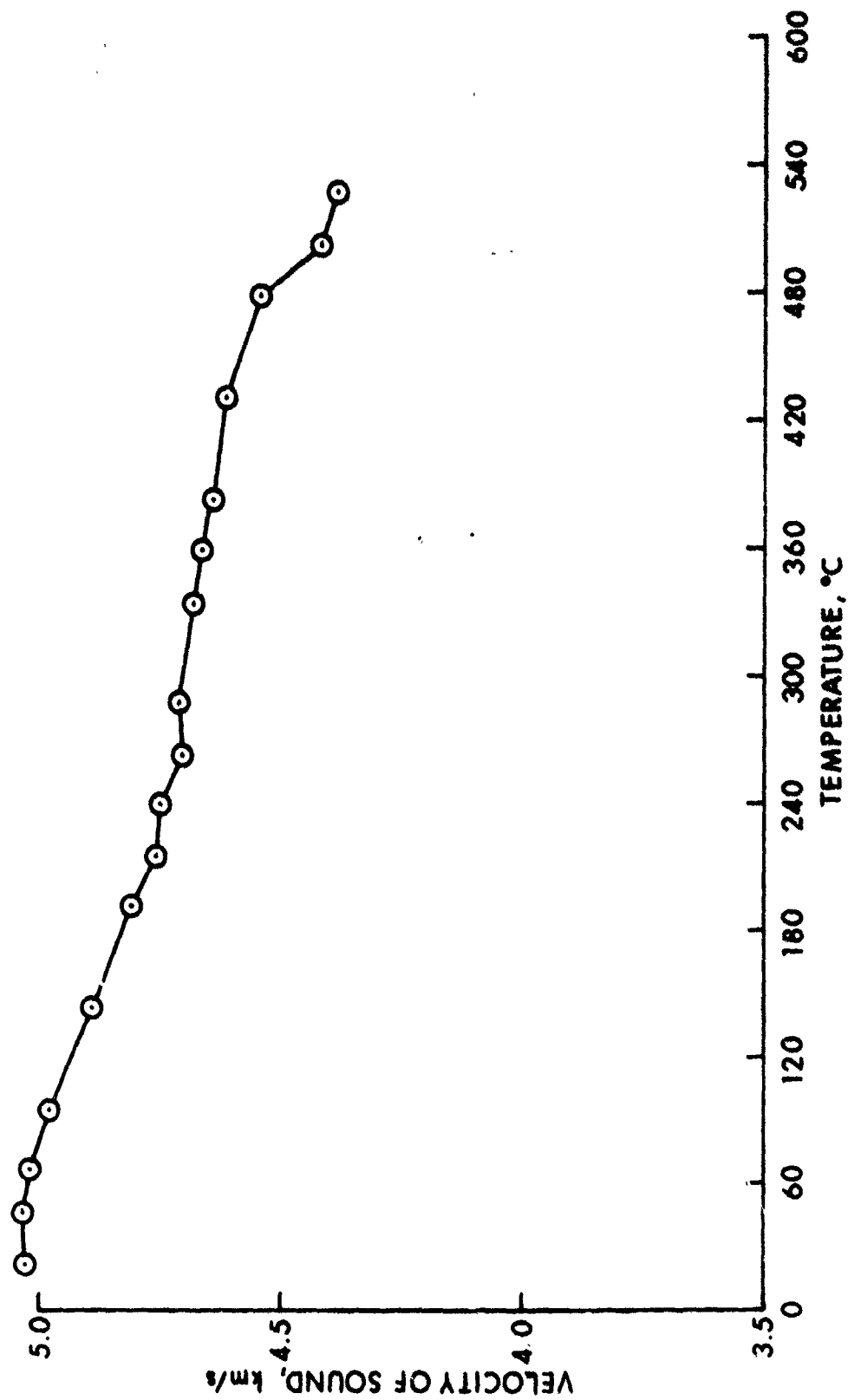


Figure 10-Velocity of Sound as a Function of Temperature for 7039-T64 Aluminum Alloy.

Our results for aluminum alloys, 2024-T3510 and 7039-T64 (Figures 3 and 9, respectively) show that Poisson's ratio decreases in a reasonably linear fashion as the temperature is increased from 25° to 500°C. Poisson's ratio for the 5083-H131 alloy (Figure 6), however, remains fairly constant from 25° to 200°C but then sharply decreases in the 200° to 500°C region. This is interpreted as a physical property of the materials tested not inconsistent with the other reported data in solids.

#### IV. CONCLUSIONS

A sonic method has been used to make dynamic measurements of Young's modulus, the shear modulus, Poisson's ratio, and the velocity of sound as a function of temperature for three aluminum alloys, 2024-T3510, 5083-H131 and 7039-T64. The results at 22°C compare favorably with similar data garnered from quasi-static tests of specimens made from the same heats of material as used for the sonic tests.

In general, the elastic constants of these three alloys decreased as the temperature was increased.



## REFERENCES

1. Instruction Manual for Model SR-200 Elastomat Instrument, Magnaflux Corporation, 7300 West Lawrence Avenue, Chicago, Illinois.
2. R. F. Benck, G. L. Filbey and E. A. Murray, BRL Memorandum Report in publication, "Quasi-Static Compression Stress-Strain Curves---IV 2024-T3510 and 6061-T6 Aluminum Alloys, Ballistic Research Laboratories, APG, MD.
3. R. F. Benck and E. A. Murray, Jr., BRL Memorandum Report #2480, "Quasi-Static Compression Stress-Strain Curves---III, 5083-H131 Aluminum", Ballistic Research Laboratories, APG, MD, May 1975. (AD #004159L)
4. E. A. Murray, Jr., BRL Memorandum Report #2589, "Quasi-Static Compression Stress-Strain Curves---II, 7039 Aluminum," Ballistic Research Laboratories, APG, MD, February 1976. (AD #B009646L)
5. J.W.S. Rayleigh, The Theory of Sound, Vol. 1, Dover Publications, New York, N.Y., 1945, p. 252.
6. D. Gerlich and E. S. Fisher, J. Phys. Chem. Solids, 30, 1197 (1969).
7. P. M. Sutton, Phys. Rev., 91, 816 (1953).
8. F. Garofalo, Trans. ASME, J. Basic Ed., 82, 867 (1960).
9. J. Wulf and W. P. Brown, Eds., "Aerospace Structural Metals Handbook", AFML-TR-68-115, Mechanical Properties Data Center, Belfour Stulen, Inc., 1974.
10. F. L. Everett, J. Appl. Phys., 15, 592 (1944).
11. J. R. Asay and A. H. Guenther, J. Appl. Phys., 38, 4086 (1967).

# DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>
2	Commander Defense Documentation Center ATTN: DDC-TCA Cameron Station Alexandria, VA 22314	1	Commander US Army Electronic Proving Ground ATTN: Tech Lib Fort Huachuca, AZ 85613
1	Director Defense Advanced Research Projects Agency ATTN: Tech Info 1400 Wilson Boulevard Arlington, VA 22209	2	Commander US Army Missile Command ATTN: DRSMI-R DRSMI-RBL Redstone Arsenal, AL 35809
1	Commander US Army Materiel Development and Readiness Command ATTN: DRCDMA-ST 5001 Eisenhower Avenue Alexandria, VA 22333	1	Commander US Army Tank Automotive Development Command ATTN: DRDTA-RHL Warren, MI 48090
1	Commander US Army Materiel Development and Readiness Command ATTN: DRCDDL 5001 Eisenhower Avenue Alexandria, VA 22333	2	Commander US Army Mobility Equipment Research & Development Command ATTN: Tech Docu Cen, Bldg. 315 DRSME-RZT Fort Belvoir, VA 22060
1	Commander US Army Aviation Systems Command ATTN: DRSV-E 12th and Spruce Streets St. Louis, MO 63166	1	Commander US Army Armament Command Rock Island, IL 61202
1	Director US Army Air Mobility Research and Development Laboratory Ames Research Center Moffett Field, CA 94035	1	Commander US Army Watervliet Arsenal ATTN: Dr. F. Schneider Watervliet, NY 12189
2	Commander US Army Electronics Command ATTN: DRSEL-RD DRSEL-HL-CT/S, Crossman Fort Monmouth, NJ 07703	1	Commander US Army Harry Diamond Labs ATTN: DRXDO-TI 2800 Powder Mill Road Adelphi, MD 20783

# DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>
5	Commander US Army Materials and Mechanics Research Center ATTN: DRXMR-ATL DRXMR-T, J. Bluhm DRXMR-XH, J. Dignam DRXMR-XO, E. Hagge DRXMR-XP, Dr. J. Burke Watertown, MA 02172	1	Director US Army Ballistic Missile Defense Systems Office 1320 Wilson Boulevard Arlington, VA 22209
1	Commander US Army Natick Research and Development Command ATTN: DRXRE, Dr. D. Sieling Natick, MA 01762	1	Director US Army Advanced BMD Technology Center ATTN: CRDABH-5, Mr. W. Loomis P. O. Box 1500, West Station Huntsville, AL 35809
1	Director US Army TRADOC Systems Analysis Activity ATTN: ATAA-SA White Sands Missile Range NM 88002	1	Commander US Army War College ATTN: Lib Carlisle Barracks, PA 17013
1	Deputy Assistant Secretary of the Army (R&D) Department of the Army Washington, DC 20310	1	Commander US Army Command and General Staff College ATTN: Archives Fort Leavenworth, KS 66027
1	HQDA (DAMA-ARP-P, Dr. Watson) Washington, DC 20310	1	Mathematics Research Center US Army University of Wisconsin Madison, WI 53706
1	HQDA (DAMA-MS) Washington, DC 20310	3	Commander US Naval Air Systems Command ATTN: AIR-604 Washington, DC 20360
1	Commander US Army Research Office P. O. Box 12211 Research Triangle Park NC 27709	3	Commander US Naval Ordnance Systems Command ATTN: ORD-0632 ORD-035 ORD-5524 Washington, DC 20360
1	Commander US Army Ballistic Missile Defense Systems Command ATTN: SENSC, Mr. Davidson P. O. Box 1500 Huntsville, AL 35804	1	Office of Naval Research Department of the Navy ATTN: Code 402 Washington, DC 20360

# DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>
1	Commander US Naval Surface Weapons Center ATTN: Code Gr-9, Dr. W. Soper Dahlgren, VA 22448	1	Director National Aeronautics and Space Administration Manned Spacecraft Center ATTN: Lib Houston, TX 77058
1	Commander and Director US Naval Electronics Lab ATTN: Lib San Diego, CA 92152	1	Dupont Experimental Labs ATTN: Mr. J. Lupton Wilmington, DE 19801
3	Director US Naval Research Laboratory ATTN: Code 5270, F. MacDonald Code 2020, Tech Lib Code 7786, J. Baker Washington, DC 20360	7	Sandia Laboratories ATTN: Mr. L. Davison Div 5163 Dr. C. Harness H. J. Sutherland Code 5133 Code 1721 Dr. P. Chen Albuquerque, NM 87115
1	AFATL (DLY) Eglin AFB, FL 32542	5	Brown University Division of Engineering ATTN: Prof R. Clifton Prof H. Kolsky Prof A. Pipkin Prof P. Symonds Prof J. Martin Providence, RI 02192
1	AFATL (DLDG) Eglin AFB, FL 32542	5	California Institute of Technology Div of Engineering and Applied Science ATTN: Dr. J. Milowitz Dr. E. Sternberg Dr. J. Knowles Dr. T. Coguhey Dr. R. Shield Pasadena, CA 91102
1	AFATL (DLDL, MAJ J.E. Morgan) Eglin AFB, FL 32542		
1	RADC (EMTLD/Lib) Griffiss AFB, NY 13440		
1	AUL (3T-AUL-60-118) Maxwell AFB, AL 36112		
1	Director Environmental Science Service Administration US Department of Commerce Boulder, CO 80302		
1	Director Jet Propulsion Laboratory ATTN: Lib (TDS) 4800 Oak Grove Drive Pasadena, CA 91103		

# DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>
4	Carnegie Mellon University Department of Mathematics ATTN: Dr. D. Owen Dr. M. E. Gurtin Dr. B. Coleman Dr. W. Williams Pittsburg, PA 15213	1	Massachusetts Institute of Technology ATTN: Dr. R. Probststein 77 Massachusetts Avenue Cambridge, MA 02139
2	Catholic University of America School of Engineering and Architecture ATTN: Prof. A. Durelli Prof. J. McCoy Washington, DC 20017	1	Michigan State University College of Engineering ATTN: Prof. W. Sharpe East Lansing, MI 48823
1	Harvard University Division of Engineering and Applied Physics ATTN: Dr. G. Carrier Cambridge, MA 02138	1	New York University Department of Mathematics ATTN: Dr. J. Keller University Heights New York, NY 10053
2	Iowa State University Engineering Research Lab ATTN: Dr. G. Mariboli Dr. A. Sedov Ames, IA 50010	1	Stanford Research Institute Poulter Laboratory 333 Ravenswood Avenue Menlo Park, CA 94025
5	The Johns Hopkins University ATTN: Dr. J. Ericksen Dr. J. Bell Dr. R. Green Dr. C. Truesdell Dr. R. Pond 34th and Charles Streets Baltimore, MD 21218	1	North Carolina State University Dept of Engineering Mechanics ATTN: Dr. W. Bingham P. O. Box 5071 Raleigh, NC 27607
3	Lehigh University Center for the Application of Mathematics ATTN: Dr. E. Varley Dr. R. Rivlin Prof. M. Mortell Bethlehem, PA 18015	2	Pennsylvania State University Engineering Mechanical Dept ATTN: Dr. R.M. Haythornthwaite Prof. N. Davids University Park, PA 16802
		2	Forrestal Research Center Aeronautical Engineering Lab Princeton University ATTN: Dr. S. Lam Dr. A. Eringen Princeton, NJ 08540
		1	Purdue University Inst for Mathematical Sciences ATTN: Dr. E. Cumberbatch Lafayette, IN 47907

# DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>
2	Rice University ATTN: Dr. R. Bowen Dr. C. C. Wang P. O. Box 1892 Houston, TX 77001	1	University of Delaware Dept of Mechanical Engineering ATTN: Prof. J. Vinson Newark, DE 19711
1	Southern Methodist University Solid Mechanics Division ATTN: Prof. H. Watson Dallas, TX 75221	3	University of Florida Dept of Engineering Science and Mechanics ATTN: Dr. C. A. Scianmarilla Dr. L. Malvern Dr. E. Walsh Gainesville, FL 32601
2	Southwest Research Institute Department of Mechanical Sciences ATTN: Dr. U. Lindholm Dr. W. Baker 8500 Culebra Road San Antonio, TX 78228	2	University of Houston Dept of Mechanical Engineering ATTN: Dr. T. Wheeler Dr. R. Nachlinger Houston, TX 77004
1	Stanford University ATTN: Dr. E. H. Lee Stanford, CA 94305	1	University of Illinois Dept of Theoretical and Applied Mechanics ATTN: Dr. D. Carlson Urbana, IL 61801
1	Tulane University Dept of Mechanical Engineering ATTN: Dr. S. Cowin New Orleans, LA 70012	2	University of Illinois at Chicago Circle College of Engineering Dept of Materials Engineering ATTN: Prof. A. Schulta D. T. C. T. Ting P. O. Box 4348 Chicago, IL 60680
2	University of California ATTN: Dr. N. Carroll Dr. P. Naghdi Berkeley, CA 94704		
1	University of California Dept of Aerospace and Mechanical Engineering Sciences ATTN: Dr. Y. C. Fung P. O. Box 109 La Jolla, CA 92037	1	University of Iowa ATTN: Dr. K. Valanis Iowa City, IA 52240
1	University of California Department of Mechanics ATTN: Dr. R. Stern 504 Hilgard Avenue Los Angeles, CA 90024	4	University of Kentucky Dept of Engineering Mechanics ATTN: Dr. M. Beatty Prof. O. Dillon, Jr. Prof. P. Gillis Dr. D. Leigh Lexington, KY 40506

# DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>
2	The University of Maryland Dept of Mechanical Engineering ATTN: Prof. J. Tang Dr. J. Dally College Park, MD 20742	4	University of Texas Dept of Engineering Mechanics ATTN: Prof. H. Calvit Dr. M. Stern Dr. M. Bedford Prof. Ripperger Austin, TX 78712
1	University of Minnesota Dept of Engineering Mechanics ATTN: Dr. R. Fosdick Minneapolis, MN 55455	1	University of Washington Department of Mechanical Eng ATTN: Prof. J. Chalupnik Seattle, WA 98105
1	University of Notre Dame Dept of Metallurgical Engineering and Materials Sciences ATTN: Dr. N. Fiore Notre Dame, IN 46556	2	Yale University ATTN: Dr. B. Chu Dr. E. Onat 400 Temple Street New Haven, CT 96520
1	University of Pennsylvania Towne School of Civil and Mechanical Engineering ATTN: Prof. Z. Hashin Philadelphia, PA 19105		<u>Aberdeen Proving Ground</u>  Marine Corps Ln Ofc Dir, USAMSAA